

ENERGY BANDS

~~The free electron theory of metals discussed in the previous chap~~
~~ter assumed that~~ A conduction electron in a metal crystal experian
ces a constant (zero) potential and is completely free to move about
in the crystal, restrained only by the surface of the crystal.
Obviously this is a very drastic assumption and does not seem
to be at all reasonable. Nevertheless the theory has certainly
been able to account for several of the properties of metals. e.g
specific heat paramagnetism etc Yet there are several other proper
ties for which this model cannot help the least. For example it
cannot help us to distinguish a metal (or a conductor) from a
nonmetal (or an insulator); the resistivity of a good conductor
at low temperatures may be $\sim 10^{-8}$ ohm-cm and that of a good
conductor may be as high as 10^{22} ohm-cm. Further semi-condu
ctor do not find any explanation on the basis of theory. There are
several other properties too which have similarly been treated
by the free electron theory. The shortcomings of the theory are
to traced in the oversimplified potential on which it is based.

A more reasonable approximation of the potential experianced
by an electron in passing through the crystal is one which is
perfectly periodic with the period of the lattice i.e one of
the type shown in fig 1. It may be thought of as arising from
the periodic distribution of the positive charge associated with
the ion cores situated on the lattice sites, plus the constant
(average) contribution due to all other free electrons of the
crystal. The latter contribution to the potential accounts in
an average sense the interaction effects of the single electrons
with all others. The periodicity character of the potential exten
ds to infinity in all direction inside the crystal. At the surface
of the crystal it is interrupted however and the potential there
looks somewhat as shown at the right hand edge of the figure.
this is because the lattice spacing will not be quite uniform here
there. We shall however ignore this irregularity and assume that it

that it is perfectly periodic \otimes right from the site of the surface. We now describe the behaviour of the electron in this potential using one electron - approximation throughout. This is done by finding the electron wave functions -

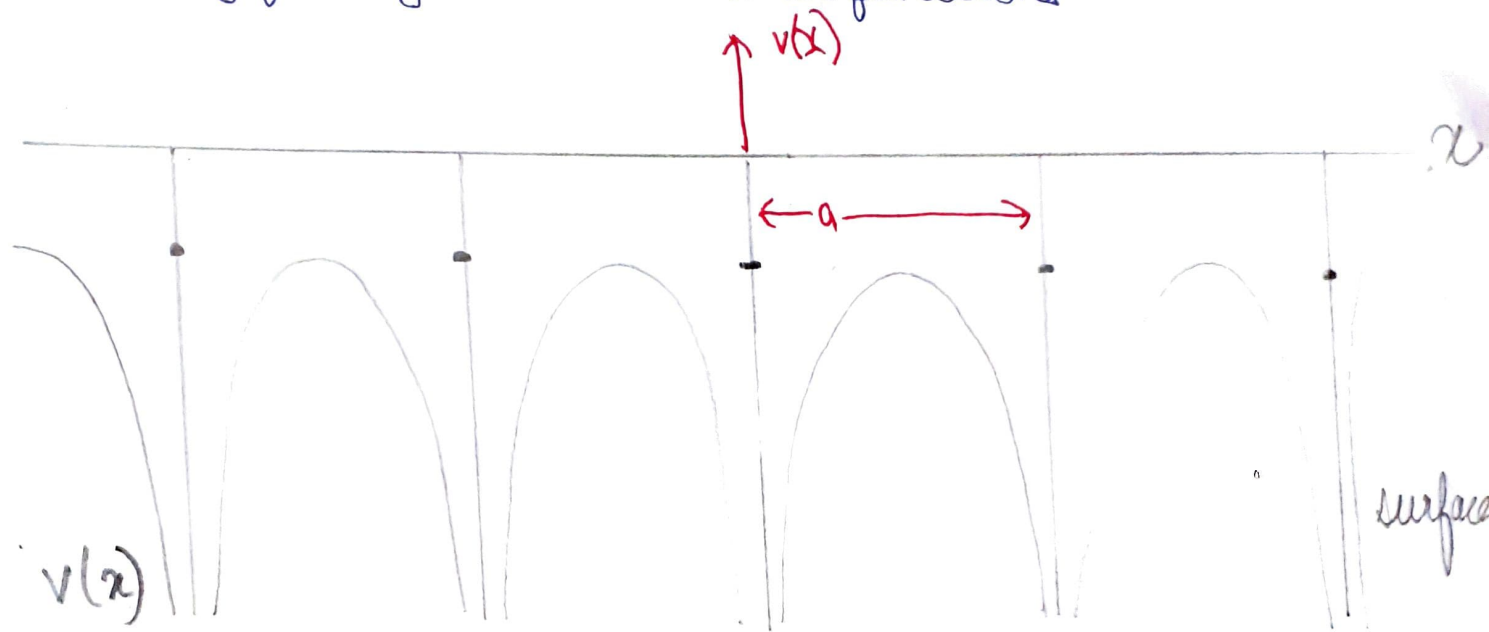


Fig 1 One dimensional representation of the potential experienced by an electron in a perfectly periodic lattice of constant a showing a sharp fall when electron approaches a positively charged nucleus.